Coda Q in the eastern Caribbean, West Indies

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SUMMARY

Coda Q, Q_c , has been estimated from seismograms of local earthquakes recorded on short-period seismographs on some of the eastern Caribbean islands of the Lesser Antilles arc, West Indies, using the S-S single-scattering model. The region was subdivided into four distinct subregions in order to investigate lateral variations in Q_c . The Q_c values exhibit a strong frequency dependence in the frequency band 1.5 to 16 Hz, with calculated coda Q at 1 Hz, Q_o , ranging from a minimum of 97 in the Dominica area to a maximum of 145 in the Leewards. The degree of frequency dependence is also largest in the Dominica area (n = 1.09) and smallest in the Leewards (n = 0.82). Although there appears to be some lateral and depth variation of both Q_o and n in the region, this variation does not seem to be very significant.

Key words: Caribbean, coda Q, earthquakes, seismograms.

1 INTRODUCTION

Attenuation of seismic waves, customarily described by the dimensionless parameter Q, called the specific quality factor, expresses the wave-amplitude decay that occurs when a wave propagates through real media and cannot be attributed to geometrical spreading. Seismic-wave attenuation is a combination of two different loss mechanisms: anelastic absorption, the loss of elastic energy to heat or other forms of energy, and scattering, the deflection and/or mode conversion of seismic energy due to randomly distributed inhomogeneities in the transmitting medium (Dainty 1981). However, according to Dainty (1981), the effects of intrinsic and scattering attenuation cannot be directly separated because of similarity in their mathematical form.

Seismic-wave attenuation varies spatially (e.g. Sutton, Mitronovas & Pomeroy 1967; Cheng & Mitchell 1981; Singh & Herrmann 1983; Jin & Aki 1988) and may also be frequency dependent (Mitchell 1980; Rovelli 1984; Kvamme & Havskov 1989), with the degree of frequency dependence varying from region to region (Mitchell 1981; Pulli & Aki 1981). Consequently, the degree of spatial variation of both attenuation and its frequency dependence may be used to infer the nature of the material conditions in the earth.

Although seismic-wave attenuation is an important parameter, knowledge of which is, for example, essential for the prediction of earthquake ground motion in seismic-hazard analyses, its nature is not well understood. Furthermore, it is difficult to measure, especially in the frequency band 1 to 30 Hz, frequencies of interest in short-period seismology and structural engineering. Hough et al. (1988), following the categories recognized by Cormier

(1982) in teleseismic studies, classified methods used to study high-frequency attenuation at near and regional distances into four broad classes. These include methods which cancel the seismic source, methods which make assumptions about the source, coda methods and time-domain methods. Many recent determinations of attenuation using local earthquakes have involved the use of coda methods because of their simplicity and ease of application.

Coda waves comprise the latter part of seismograms, the part after all the direct waves such as P, S and surface waves have arrived (Herraiz & Espinosa 1987). Theoretical and observational studies on coda waves generally seem to suggest that the coda is produced by the interaction between primary waves and small-scale lithospheric heterogeneities. Scattered body waves can also be generated by topography (Spudich & Bostwick 1987) while an irregular low-velocity surface layer will convert and scatter body waves to surface waves (Levander & Hill 1985).

The most widely applied coda method is that formulated by Aki (1969) and extended by Aki & Chouet (1975) and Sato (1977). It considers the S-wave coda as consisting of single, backscattered S-waves from randomly distributed heterogeneities in the lithosphere. The envelopes of the codas of narrow, bandpass-filtered seismograms can then be used to determine the average Q for the medium for the particular frequency bands. The single-scattering model has been used to determine attenuation in many regions of the world (e.g. Rautian & Khalturin 1978; Roecker et al. 1982; Pulli 1984; Havskov et al. 1989; Ambeh & Fairhead 1989) and to investigate temporal changes in coda attenuation as a possible tool for earthquake prediction (e.g. Jin & Aki 1986; Lee et al. 1986; Novelo-Casanova, Berg & Helsley 1990).

Although this simple model seems to explain much of the

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character of observed coda, there are still significant disagreements, especially in the details of the modelling process. For example, a point of great contention is how the coda Q should be interpreted. Coda Q as originally formulated was thought to be a reflection of the scattering effect only (Aki 1969). Aki (1980a) and many others, from comparisons of coda Q and shear wave Q, have suggested that coda Q is more closely related to intrinsic rather than scattering attenuation. This view has been supported by results of analyses by Wu (1985) and Frankel & Wennerberg (1987) using energy flux models. Langston (1989) has, however, shown in the analysis of long-period Rayleigh waves in western North America that coda decay with time, which is used to obtain Q, cannot be used to discriminate between coda mechanisms, i.e. scattering or anelastic absorption.

The eastern Caribbean is a tectonically complex area which includes a subduction zone, island arc and active volcanoes. Earthquakes occurring in the area have focal depths from near surface to about 200 km and are monitored by short-period seismographs operated by the Seismic Research Unit of the University of the West Indies, Trinidad, and the 'observatoires Volcanologiques' in Guadeloupe and Martinique. No quantitative studies of seismic-wave attenuation in the eastern Caribbean have been made to date. In this paper, we investigate the spatial variation of seismic-wave attenuation and its frequency dependence in the eastern Caribbean using the Sato (1977) extension to the S-S single scattering coda model of Aki & Chouet (1975).

2 MODEL, DATA AND ANALYSIS

2.1 The model

In the single, backscattering model of Aki & Chouet (1975), coda waves are considered as being composed of the superposition of backscattered body waves from numerous randomly distributed heterogeneities in the lithosphere. The model assumes that the earthquake and the station are coincident, i.e. the scatterers are at large distances compared to the source–receiver distance. According to Aki & Chouet (1975), coda amplitude, $A(f \mid t)$, at frequency, f, and lapse time (traveltime), t, is given by

$$A(f \mid t) = C(f)t^{-\alpha} \exp\left(-\pi f t/Q_c\right) \tag{1}$$

where C(f) represents the coda source factor, α is a constant that depends on geometrical spreading and takes values of 1.0, 0.5 and 0.75 for body wave, surface wave and diffusion scattering respectively, and Q_c is the coda quality factor.

Aki (1980b), based on reported results of good agreement between coda Q and shear wave Q (e.g. Rautian & Khalturin 1978; Aki 1980a), concluded that coda waves are made up primarily of backscattered S waves. This close agreement between S-wave Q and coda Q has been confirmed by other workers (e.g. Roecker $et\ al.$ 1982; Del Pezzo $et\ al.$ 1985; Rebollar, Traslosheros & Alvarez 1985; Kvamme & Havskov 1989). Consequently, we assume a spreading parameter of $\alpha=1$. It must, however, be mentioned that Herrmann (1980) also found good

agreement at 1 Hz between coda Q and Q from Lg waves.

The assumption in the model of Aki & Chouet (1975) that the source and the receiver are located at the same point is acceptable for coda waves recorded long after the passage of the primary waves. In fact, Rautian & Khalturin (1978) state that eq. (1) is valid only for lapse times greater than twice the S-wave traveltime. However, analysis in this region of the coda is often difficult because of an inadequate signal-to-noise ratio or short recording times. Sato (1977) extended the above single-scattering model to incorporate source-receiver offset, thus allowing one to begin coda analysis immediately after the shear wave arrival. The coda-wave relationship in the case of non-coincident source and receiver may be stated as

$$A(r, f \mid t) = C(f)K(r, a) \exp(-\pi f t/Q_c)$$
(2)

where $a=t/t_s$, t_s is the S-wave lapse time, r is the source-receiver distance, $K(r,a)=(1/r)\{(1/a)\ln{[(a+1)/(a-1)]}\}^{0.5}$ and all the other symbols have the same meaning as in eq. (1). Taking natural logarithms of eq. (2) and rearranging terms, we obtain

$$\ln [A(r, f \mid t)/k(r, a)] = \ln C(f) - (\pi f/Q_c)t.$$
(3)

For narrow-bandpass filtered seismograms, C(f) is a constant and hence by performing a linear regression of the term on the left-hand side of eq. (3) versus t, Q_c can be determined from the slope which is equal to $-\pi f/Q_c$.

2.2 Data

In order to make a regional comparison of coda Q in the eastern Caribbean, we searched the data base of the Seismic Research Unit (SRU) of the University of the West Indies, Trinidad, for suitable events/seismograms recorded during the period May 1989 to June 1991. The SRU has operated a telemetred network of short-period (1 s) vertical component seismic stations in the English-speaking eastern Caribbean islands since 1987. Data digitized at a rate of 100 samples per/s and 12-bit resolution has been recorded on personal computers. Events/seismograms were selected on the basis of such factors as spatial distribution, absence of spikes, good signal-to-noise ratio characteristics, and epicentral distances less than about 70 km.

The final data set used in this study consists of 73 earthquakes with signal duration magnitudes, MD, ranging from 2.3 to 3.7 and focal depths from 1 km to 183 km. The earthquake epicentres and station locations are plotted in Fig. 1 while detailed information on the events and stations are listed in Tables 1 and 2 respectively. Ideally, we would have liked the epicentres to be distributed uniformly along the island arc but, unfortunately, this is not the case. Events are concentrated at the northern and southern ends and this, to a certain extent, is a reflection of the contemporary seismicity pattern in the eastern Caribbean. The lack of data in the Guadeloupe and Martinique areas is due to the unavailability of seismograms for stations on these islands while fewer earthquakes occur in the region from Grenada to St Lucia. Using the available earthquake and station data, we subdivided the eastern Caribbean into four subregions as shown in Fig. 1 and Table 1.

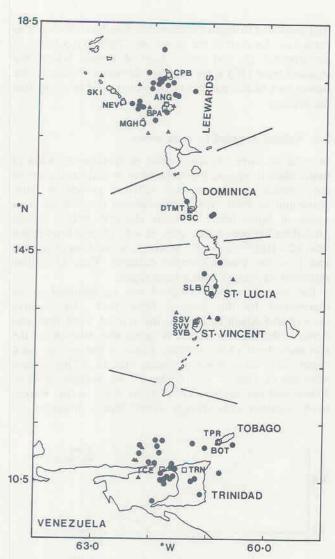


Figure 1. Map showing the earthquake epicentres and stations used in this study. Dots are shallow earthquakes $(0 \le Z \le 70 \text{ km})$, triangles are intermediate depth earthquakes (70 < Z < 200 km) and squares are seismic stations. Approximate boundaries of the four subregions are also shown.

Analysis

Each seismogram time series was first bandpass filtered over eight frequency bands centred at 1.5, 2, 3, 4, 6, 8, 12 and 16 Hz, with bandwidths of 1, 2, 2, 4, 4, 8, 8, and 16 Hz respectively, using an eight-pole, phase-free Butterworth filter. Starting at the S arrival, the root-mean-square (rms) amplitudes in each window were determined for the data in each frequency band, with the window sliding across the time series at 1 s intervals. Time-window lengths for the rms averaging of 8s (for centre frequencies of 1.5, 2, 3, 4 and 6 Hz) and 5 s (for centre frequencies 8, 12 and 16 Hz) were chosen so as to smooth out as much as possible irregularities in the amplitudes of the arrivals. The left-hand side of eq. (3) was then evaluated and plotted against lapse time. From the plot, the linear portion, which had to be at least 30 s long, was visually selected and a straight line fitted to it

Table 1. Parameters of events used in the coda-Q analysis.

Trinidad/Tobago (TT) Region Date Time Lat. Lon. Depth Md Stations DDMM-YY-HRMN SEC 01061989 0757 48.17 10.55 61.63 TRN 27061989 52.14 10.56 62.17 76 3.2 TRN TCE 04071989 0716 35.90 91 3.8 TCE 10071989 1230 03.46 10.65 3.0 TRN 31071989 0820 10.75 61.62 39 3.1 TRN 03101989 1903 42.47 10.49 61.27 44 TRN 20111989 2307 38.70 44 3.5 BOT 29111989 1020 00.44 11.10 61.86 2.9 TCE 20121989 1030 04.89 10.85 62.21 87 20121989 21121989 1815 43.38 10.83 62.00 3.2 48 TRN TCE 13.02 29.52 1516 11.21 61.89 15 TCE 23121989 0355 10.16 61.93 TCE 19011990 0742 23.21 10.72 61.55 41 3.2 TRN TCE 31011990 2214 0915 59.73 35.79 10.28 2.6 TRN 62.16 9 2.9 14041990 2232 34.37 10.99 61.82 3.0 TRN TOF 26041990 0453 22.27 11.20 61.77 TCE 04051990 26.06 61.58 39 2.5 TRN 22071990 0350 27.40 10.51 2.4 TRN 05081990 1103 54.29 10.46 61.73 10 2.9 TRN 07091990 0749 36.07 61.60 61 3.4 TRN TCE 17091990 1207 43.97 61.90 3.5 44 TRN 22091990 0058 16.85 11.08 57.35 10.52 61.04 33 TRN 20111990 1240 61.80 26 3.1 TRN 29111990 22.81 10.64 61.79 49 3.0 TRN 17121990 0725 29.46 62.11 76 3.1 TCE 15011991 1555 14.62 10.54 61.73 TRN 03021991 0311 57.97 10.55 61.20 40 3.0 TRN 13031991 1146 07.16 10.98 62.17 3.0 68 TCE 30041991 2224 08.79 TRN 14061991 0155 46.82 10.58 61.68 St. Vincent/St. Lucia (SVL) Region 09081989 2207 23.63 14.32 60.83 3.4 55.85 13.44 145 SVV SSV SVB 61.56 19071990 0624 28.30 13.37 60.99 128 3.1 25081990 0509 31.78 14.04 60.59 71 3.4 SLB 30091990 0632 22.90 13.92 3.2 60.89 39 SLR 13.79 0358 42.67 02101990 60.97 20 SLB 25121990 2108 44.84 13.36 10021991 1834 39.75 14.13 3.0 61.10 SLB Dominica Region 26051989 0216 17.85 15.39 DTMT DSC 05121989 2324 09.88 15.14 15 3.1 DTMT 12121989 0256 09.39 15.17 60.95 15 2.7 Leewards Region 12051989 0607 25.17 17.00 26051989 0124 23.59 17.05 07061989 0525 41.79 16.56 62.30 19 3.2 NEV SKI 62.26 3.7 BPA ANG 62.11 146 3.4 20061989 1638 38.46 17.64 2.9 38 NEV BPA 23061989 0708 23.66 17.13 18 3.1 NEV 01071989 1321 50.33 0801 15.59 17.03 62.21 11 BPA 16071989 62.40 2.4 NEV 17071989 1034 15.30 62.09 105 MGH BPA 17071989 2102 56.96 09.36 17.32 17.57 61.30 3.1 21071989 0538 183 3.2 SKI 03081989 1753 15.53 27.92 16.99 62.29 3.0 MGH 0248 17.44 3.2 61.94 40 BPA 29.15 21.45 06.96 1906 0213 09081989 62.24 96 BPA 14081989 16.80 61.99 30081989 1032 17.54 61.85 64 3.5 BPA 07111989 1305 14.79 17.43 78 BPA 30111989 1435 57.28 17.47 BPA 06011990 61.79 61.76 1630 47.15 16.95 20 2.9 09011990 0021 35.06 16.59 128 ANG 06021990 1126 08.91 17.48 61.90 13 3.5 BPA 17.28 17.37 47.70 17.05 06021990 1133 61.71 3.0 17021990 1630 61.67 71 3.2 RPA 25041990 0625 28.03 16.98 83 BPA MGH 03061990 0951 22071990 0847 39.59 17.42 56.65 18.05 61.78 CPB 61.85 25 29 2.9 CPR 26071990 17.53 3.5 BPA 03091990 0022 54.44 17.46 62.04 28.68 17.26 40.76 17.23 11091990 0848 61.65 35 3.3 BPA 0336

61.59

62.26

24101990

1002

27101990 1952 42.51 17.10

23.23

46

3.0

BPA

BPA

Table 2. Listings of stations used in the coda-Q analysis.

Code	Name	Lat.(°N)	Lon.(°W)	Alt.(m
TRN TCE BOT TPR SVB SVV SSV SLB DSC DTMT MGH NEV SKI BPA ANG CPB	St. Augustine, Trinidad Chacachacare, Trinidad Bacolet, Tobago Prospect, Tobago Belmont, St. Vincent Wallibou, St. Vincent Summit, St. Vincent Belfond, St. Lucia Scott's Head, Dominica Tete Morne, Dominica St. George's Hill, Monserrat Gingerland, Nevis Bayfords, St. Kitts Boggy Peak, Antigua Frias Hill, Antigua Codrington, Barbuda	10.65 10.70 11.16 11.18 13.27 13.32 13.33 13.82 15.21 15.23 16.72 17.13 17.13 17.04 17.15 17.64	61.40 61.75 60.72 60.78 61.25 61.21 61.19 61.04 61.35 62.21 62.57 62.74 61.86 61.82	24 240 30 245 282 243 824 600 50 496 324 306 396 27

by least squares. From the slope of the line, Q_c was calculated. By using only linear windows which were at least 30 s long, we hope to minimize the contribution of temporal small-scale variations in coda amplitude which may be caused by interference effects, secondary arrivals, or site conditions.

Fig. 2 is an example of the application of this analysis procedure. Only Q_c values obtained from least-squares fits with correlation coefficients greater than or equal to 0.95 were retained. The arbitrary value of 0.95 seems to represent an acceptable compromise between rejecting too much data and obtaining a high scatter in individual Q values for a particular region. For each station, an average coda-Q value was calculated at each frequency for the data,

split according to depth ranges where possible. This was also carried out for each of the subregions. Table 3 is a listing of the average \mathcal{Q}_c and their standard errors, where the standard error (SE) is the standard deviation divided by the square root of the number of \mathcal{Q}_c values used in calculating the average.

2.4 Volume sampled by coda waves

In order to carry out meaningful comparisons of coda Q from different regions, it is imperative to make estimates of the volumes sampled by the different groups of data. According to Pulli (1984), the volume sampled by coda waves at lapse time, t, is an ellipsoid whose surface projection has semi-major axis, $a1 = V_s t/2$, and semi-minor axis, $a2 = [(a1)^2 - (r^2/4)]^{0.5}$ where V_s is the S-wave velocity and r is the source-receiver distance. Thus Q_c values represent an average over a large region.

The average volume sampled can be assumed to be represented by the average lapse time, Tav, where tav = tstart + Δt win/2; tstart is the starting lapse time and Δt win is the window length. A reasonable estimate of the maximum depth of the volume, Zmax, is the average focal depth, Zav, for a group of events plus a2. Using S-wave velocities of 4 km s^{-1} and 4.5 km s^{-1} for shallow ($0 \le z \le 70 \text{ km}$) and intermediate (Z > 70 km) depth events respectively, together with average source-station distances and

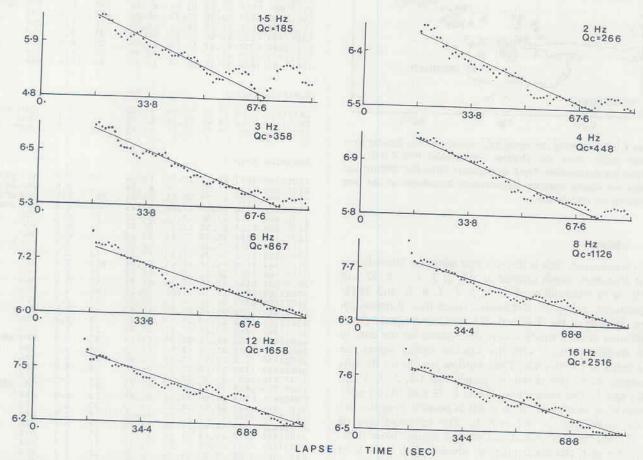


Figure 2. Example of coda-Q analysis as applied to station TRN seismogram for event of 22071990 0350 UTC. The plot is for the quantity $\ln \left[A(r, f \mid t)/k(r, a)\right]$ versus lapse time, t. The straight lines show the portions chosen to determine Q_c .

Table 3. Average Q_c values and their standard errors. Values in brackets represent the number of Q used in averaging. T.T—Trinidad/Tobago; St V't—St Vincent; DOM—Dominica; Lwds—Leewards. S: shallow events; I: intermediate depth events; A: all events.

Station				FREQ	UENCY			
Region	1.5	2.0	3.0	4.0	6.0	8.0	12.0	16.0
TRN(S)	194±16 (4)	259±13 (15)	321±17 (16)	398±15 (20)	548±26 (20)	750±38 (19)	1037±72 (14)	1484±122 (13)
TRN(I)	±	*1	∌.	362 (1)	449 (1)	-	*	
TRN(A)	194±16 (4)	259±13 (15)	321±17 (16)	396±14 (21)	544±25 (21)	750±38 (19)	1037±72 (14)	1484±122 (13)
TCE(S)	Jan e	211±7 (2)	369±21 (7)	442±19 (9)	664±25 (10)	822±42 (10)	1137±148 (3)	1524±174 (3)
TCE(I)	152 (1)	298±106 (2)	358±39 (3)	404:5	576±45 (4)	805±69 (4)	1247±294 (4)	1659±534 (3)
TCE(A)	152 (1)	255±50 (4)	366±18 (10)	433±15 (12)	639±24 (14)	817±35 (14)	1200±168 (7)	1592±253 (6)
BOT(S)	176 (1)	163 (1)	243 (1)	294 (1)	304 (1)		*	
TPR(S)		142	207	331 (1)	522 (1)	814	1268	1675 (1)
T.T(S)	190±13 (5)	243±13 (19)	327±14 (25)	405±12 (31)	576±22 (32)	776±28 (30)	1067±61 (18)	1502±97 (17)
T.T(I)	152 (1)	298±106 (2)	358±39 (3)	394±11 (4)	551±43 (5)	805±69 (4)	1247±294 (4)	1659±534 (3)
T.T(A)	184±12 (6)	248±14 (21)	330±13 (28)	404±11 (35)	573±20 (37)	779±26 (34)	1099±70 (22)	1526±107 (20)
SVV(I)		350 (1)	435 (1)	463 (1)	631 (1)	855 (1)	1022	1381
SSV(I)	Autoria in Au		386 (1)	433	523 (1)	718 (1)	1064	1506
SVB(I)			351±74 (2)	450±88 (2)	546±68 (2)	741±80 (2)	1367 (1)	2150 (1)
SLVt(A)	2	350 (1)	381±36 (4)	449±36 (4)	561±36 (4)	764±45 (4)	1144±112 (3)	1679±238 (3)
SLB(S)	*	210±16 (2)	296±20 (4)	369±29 (4)	638±21 (2)	754±33 (3)	1072±145 (3)	1464±192 (4)
SLB(I)	157 (1)	197 (1)	344 (1)	467 (1)	762 (1)	849 (1)	1162 (1)	1964 (1)
SLB(A)	157 (1)	206±10 (3)	306±18 (5)	389±30 (5)	679±43 (3)	777±33 (4)	1095±105 (4)	1564±179 (5)
SVL(A)	157 (1)	242±37 (4)	339±22 (9)	415±24 (9)	612±35 (7)	771±26 (8)	1116±71 (7)	1607±134 (8)
DSC(S)		207 (1)	295 (1)	368 (1)	1 112 -111			3.5
DTMT(S)	Hw" har	236 (1)	270 (1)	469±81 (2)	757±209 (2)	1023±140 (3)	1354	1870 (1)
DOM(A)		221±14 (2)	282±13 (2)	435±58 (3)	757±209 (2)	1023±140 (3)	1354	1870 (1)
MGH(S)	ALL PLANTS	#	398 (1)	400	752 (1)	1039	1641	pe - 1 3 m
MGH(I)	207±53 (2)	306±1 (3)	373±33 (3)	486±42 (3)	730±79 (3)	1104±156 (3)	1818±872 (2)	2325±1019 (2)
MGH(A)	207±53 (2)	306±1 (3)	380±24 (4)	465±37 (4)	735±56 (4)	1088±111 (4)	1759±507 (3)	2325±1019 (2)
NEV(S)	i i inim	269 (1)	273±27 (4)	345±34 (4)	423±111 (2)	1058±341 (2)	984 (1)	1236 (1)
SKI(S)	200			615 (1)	828	1255	*	Tilmen
SKI(I)	8	11/2/2011		521 (1)	872 (1)	1225	2884 (1)	3455 (1)
SKI(A)				568±47 (2)	850±22 (2)	1240±15 (2)	2884	3455 (1)
BPA(S)	216±30 (5)	296±31 (8)	352±19 (11)	480±22 (15)	655±48 (16)	805±38 (16)	1121±51 (17)	1482±88 (15)
BPA(I)	239±36 (2)	301±69 (4)	351±59 (6)	454±69 (6)	630±84 (6)	853±118 (6)	1176±119 (6)	1624±133 (6)
BPA(A)	223±23 (7)	298±29 (12)	352±23 (17)	473±24 (21)	648±41 (22)	818±41 (22)	1135±47 (23)	1523±73 (21)
ANG(S)		377 (1)	450±26 (2)	599±0 (2)	820±78 (2)	983±86 (2)	1274±290 (2)	1736±396 (2)
ANG(I)	- 11			583	580 (1)	849 (1)		11 8 T 111
ANG(A)	7.	377 (1)	450±26 (2)	593±5 (3)	740±92 (3)	938±67 (3)	1274±290 (2)	1736±396 (2)

Table 3. (Continued.)

Station			FREQUENCY						
Region	1.5	2.0	3.0%	4.0	6.0	8.0	12.0	16.0	
CPB(S)	30	~	238 (1)	302 (1)	387±33 (2)	588±25 (2)	873±158 (2)	1294	
L'wards(S)	216±30 (5)	301±26 (10)	342±18 (19)	463±22 (24)	638±41 (24)	851±44 (24)	1129±52 (23)	1486±80 (19)	
L'wards(I)	223±28 (4)	303±37 (7)	359±40 (9)	481±39 (11)	674±54 (11)	955±84 (11)	1508±255 (9)	1983±283	
L'wards(A)	219±19 (9)	302±21 (17)	348±17 (28)	- Y	17	**************************************	-	(9)	

lapse times, the parameters, which are a reflection of the volume sampled by coda waves in each subregion, were calculated. For example, for the shallow earthquakes in the Trinidad and Tobago region, Q_c estimates at an average lapse time of 52 s correspond to sampling volumes of about 208 km in lateral extent, 137 km in depth and $16\,500\,\mathrm{km^2}$ in surface area. Sampling volumes for shallow earthquakes in the other subregions are similar to those for the Trinidad and Tobago area. We deduce that the volumes sampled by the coda waves from shallow events in each subregion appear to be distinct, with little or no overlap. This may, however, not be the case for the coda waves of intermediate depth events which sample larger volumes.

3 RESULTS

Our results show that average Q_c values in the eastern Caribbean at a frequency of 1.5 Hz, range from 152 for intermediate depth earthquakes recorded at TCE, to about 239 for intermediate depth events recorded at BPA. At 16 Hz, the variation in Q_c is from about 1236 (NEV) to 3455 (SKI). Looking at the Q_c values listed in Table 3, there seems to be some variation within particular subregions, i.e. among stations, and between the different subregions. However, before examining the coda Q in detail for station-to-station or regional variations, we checked for other possible causes of fluctuations in Q_c values, such as window length, average lapse time, epicentral distance, focal depth and magnitude.

3.1 Variation of Q_c with window length, average lapse time, epicentral distance, focal depth and magnitude

It has been observed in many coda-Q studies that Q increases with increased lapse time and consequently, increased window length (e.g. Rautian & Khalturin 1978; Rovelli 1984; Lee et al. 1986; Kvamme & Havskov 1989). Taking into consideration the volumes sampled by coda waves as postulated by Pulli (1984), increasing coda Q with increasing lapse times has been interpreted to be due to increasing Q with depth (Roecker et al. 1982; Rovelli 1984). But Gao et al. (1983a) have suggested that multiple scattering might be responsible for the observed increase in Q, while others have attributed it to incorrect coda-model parameterization [e.g. the use of an inappropriate geometrical spreading factor, α , in eq. (1)]. We note, however, that Havskov et al. (1989) and Canas et al. (1991) did not observe any significant variation in Qc with lapse time and window length for studies in Washington State, USA, and southern Spain respectively.

 Q_c values for stations TRN and BPA were plotted, for each frequency, against each of the following variables:

window length, average lapse time, epicentral distance, focal depth and magnitude. TRN and BPA were chosen because they had relatively more data compared to the other stations. We found no obvious dependence of Q_c values at TRN or BPA on any of the above variables. Selected examples of these plots are shown in Fig. 3.

3.2 Q_c variation and frequency dependence

In most regions where coda-Q measurements have been made, a positive correlation between Q_c and frequency has been noted (e.g. Aki & Chouet 1975; Rautian & Khalturin 1978; Roecker et al. 1982; Pulli 1984; Havskov et al. 1989; Ambeh & Fairhead 1989). Frequency-dependent Q has also been observed in studies of shear wave Q using the single-station method (Aki 1980a), in an inversion of P-wave data for Q (e.g. Thouvenot 1983), and in shear wave spectral analysis (e.g. Singh et al. 1982; Rebollar et al. 1985; Kvamme & Havskov 1989). The form of this frequency dependence is generally

$$Q_c = Q_o f^n \tag{4}$$

where n has been found to lie mainly in the range 0.5 to 1.1. Stations and regions with Q_c values from at least three events were fitted to eq. (4) and the results are listed in Table 4.

In the Trinidad and Tobago region, there seems to be no significant difference between average Q_c at all frequencies for stations TRN and TCE within error limits for both shallow and intermediate depth earthquakes. This is confirmed by calculated Q_o values which lie in the narrow range 128 to 132. The variation in the index, n, is also very small: 0.83 for TRN shallow events and 0.88 for TCE shallow and intermediate depth earthquakes. This is not totally surprising since both TCE and TRN sample almost the same volume. It may also suggest that the influence of receiver site effects are minimal. A similar comparison could not be extended to the two Tobago stations, TPR and BOT, because their Q_c values are from a single earthquake only.

 Q_c at St Vincent stations (SVV, SSV, SVB) were estimated from two intermediate-depth earthquakes and are generally consistent with each other. No Q_c values from shallow earthquakes are available for these stations.

For SLB (St Lucia), average Q_c from four shallow earthquakes at 3 to 16 Hz appear to be slightly lower (by ~ 100) than those for a single intermediate depth event. $Q_o = 105$ and n = 0.94 were obtained for these shallow events. Although none of the earthquakes used for SLB was recorded at any of the St Vincent stations and vice versa, we decided, because of the paucity of suitable earthquake data in the St Vincent and St Lucia area and the overlapping coda volumes involved, to treat this area as a single

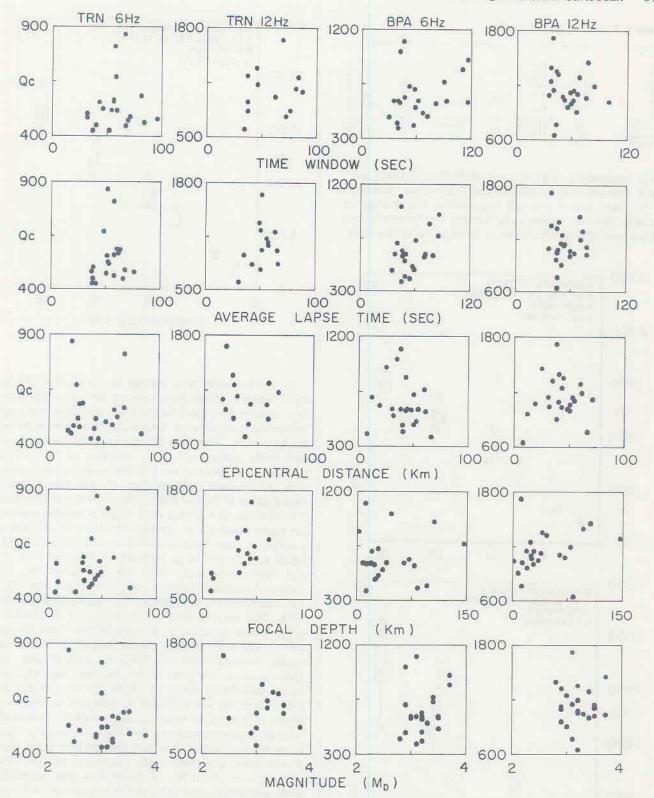


Figure 3. Selected examples of plots of the variation of Q_c at TRN and BPA as a function of window length, average lapse time, epicentral distance, focal depth and magnitude.

subregion. A Q_o of 129 was obtained for the St Vincent/St Lucia intermediate depth events compared to the 105 for the shallow events. Again, considering the uncertainties involved in determining Q and the different depths of penetration of the coda waves, this difference does not

appear very significant. The values of n, 0.89 for the intermediate depth earthquakes and 0.94 for the shallow events, are also not much different within error limits.

The three earthquakes used in the Dominica region are shallow and average Q_c at 2 and 16 Hz are 221 ± 14 and

Table 4. Calculated Q_o and n values

Station/ Region	Shallow Events Q _a n		Interm Q	ediate Events	All Events Q. n	
TRN TCE SLB DTMT NEV MGH	131 132 105 105 101	0.83:0.03 0.88:0.04 0.94:0.05 1.06:0.11 0.92:0.14	128	0.8810.08	130 131 106 105 101 133 147 209 124 119 97 141	0.83±0.03 0.88±0.03 0.96±0.04 1.06±0.11 0.92±0.14 0.98±0.07 0.82±0.03 0.73±0.07 0.87±0.02 0.91±0.04 1.09±0.09 0.85±0.03
BPA ANG	egion 105 lida 97	0.80:0.03	136 137	0.97±0.08 0.85±0.07		
TT region SVL region Dominica Leewards		0.86±0.02 0.94±0.05 1.09±0.09	124 129	0.88±0.08 0.89±0.05		
Decentus		0.8210.03	134	0.92±0.06		

1870 respectively. Two stations (DTMT and DSC) were used although DSC contributed only 3 Q_c values. Estimates of Q_o and n are 97 and 1.09 respectively. The shortage of suitable data for stations in St Vincent and Dominica may be partially attributable to the noisiness of the station sites.

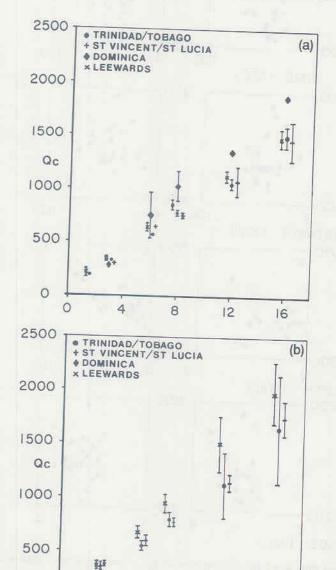


Figure 4. Average Q_c versus frequency for the different subregions (A: shallow events; B: intermediate depth events; C: all events). Error bars represent ± 1 standard error.

8

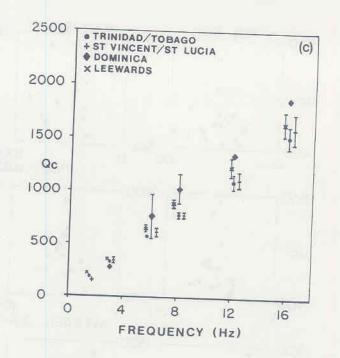
12

16

4

0

0



For the Leewards area, average Q_c for stations CPB and NEV, which are from shallow events only, generally appear to be smaller than those for the other stations in the region for the same depth range. This seems to be valid at most of the frequencies. Very high Q_c values of 2884, and 3455 at 12 and 16 Hz respectively, were obtained at SKI for the deepest event (183 km) used in this study. These compare with intermediate-depth average Q_c for this region of 1508 ± 255 at 12 Hz and 1983 ± 283 at 16 Hz. Unfortunately, a Q_c value for this 183 km depth event at another station in the region could not be determined. However, this was not a unique situation because a 105 km deep event recorded at MGH also resulted in Q_c estimates of 2690 and 3344 at 12 and 16 Hz respectively. The low Qc values for NEV compared to other Leewards stations is reflected in a Q_o of 101, compared to, for example, 152 for shallow events at BPA. This may be due to site effects or differences in sampled coda volumes. Q_o for intermediate depth events at BPA is 138, which is slightly lower than the 152 for shallow events. Although BPA and ANG are situated only about 13 km apart on the same island, Antigua, their Q_o and nvalues considering events at all depths are 209 and 0.73 (ANG) and 147 and 0.82 (BPA). This may be due to site effects at ANG since seismograms recorded at this station seem to display anomalously long codas. Average Q_c in the Leewards for both shallow and intermediate-depth events do not differ significantly within uncertainty bounds, except perhaps at 12 and 16 Hz. Q_o for shallow and intermediate depth earthquakes are 145 and 134 respectively, while n is 0.82 for shallow and 0.92 for intermediate events.

Average Q_c for shallow, intermediate and all earthquakes for the four subregions are plotted as a function of frequency in Fig. 4. For the shallow events (Fig. 4a), the main feature is the fact that Q_c for the Dominica region seems generally to be higher than those for the other regions at frequencies greater than or equal to 6 Hz. This is in spite of the fact that events in the Dominica region sample a

shallower coda volume compared to those in the other regions. Attenuation of waves with frequencies greater than about 6 Hz may, therefore, be greater in the Dominica region compared to the other areas in the eastern Caribbean. It must be stated once more that the number of events used in the Dominica region is small and consequently some caution has to be exercised in the interpretation and conclusions. For the intermediate depth earthquakes (Fig. 4b), average Q_c for the Leewards are larger than those for the Trinidad and Tobago region at all frequencies although there is a significant overlap of error bars at higher frequencies. Fig. 4(c), which shows data for all events, seems to reflect on average trends already described for the shallow and intermediate depth events.

4 DISCUSSION AND CONCLUSIONS

A comprehensive review of coda studies and the problems associated with the interpretation of Q_c was made by Herraiz & Espinosa (1987). While there seems to be no doubt that coda originates from waves scattered from lithospheric heterogeneities, there is still no commonly accepted view as to what Q_c represents. In this study, we used the extension of Sato (1977) to the single S-S backscattering model of Aki & Chouet (1975) and consequently, our interpretation of the results are ultimately constrained by the assumptions and limitations of this model.

Several studies have questioned the validity of the single-scattering approach in coda studies. According to Gao et al. (1983a, b), the effects of multiple scattering are dominant at lapse times greater than about 100 s, but Spudich & Bostwick (1987), in an analysis of Morgan Hill, California, local earthquakes, found that the early portions of their coda were dominated by multiple scattering from near-site heterogeneities. Qc as originally formulated by Aki (1969) was thought to reflect a predominantly scattering contribution. However, Frankel & Wennerberg (1987), using an energy-flux model, suggest that Q_c is a measure of intrinsic rather than scattering attenuation. The physical significance of the frequency dependence of Q_c is also a point of contention. Dainty (1981) suggested that the frequency dependence of Q_c between 1 and 20 Hz is mainly due to scattering, with anelastic attenuation being relatively frequency independent. Richards & Menke (1983) and Frankel & Clayton (1986), however, conclude that frequency dependence observed in coda analysis using the single scattering approach may be due to multiple scattering.

Empirical correlations between the coda Q at 1 Hz, Q_o , in an area, and the level of current tectonic activity in the area, have been made. Seismically active regions, or areas with a high intensity of tectonic activity, seem to be associated with low Q_o values (e.g. Aki 1980b; Roecker $et\ al.$ 1982; Singh & Herrmann 1983; Van Eck 1988; Jin & Aki 1988; Canas $et\ al.$ 1991). Correlations between the degree of frequency dependence of Q_c and the level of tectonic activity in the area of measurement have also been made in compilations of Q_c measurements by several workers (e.g. Aki 1980b; Pulli & Aki 1981; Jin, Cao & Aki 1985). In general, tectonically stable regions were found to exhibit almost no frequency dependence while active areas in which processes

such as folding, faulting or subduction are likely to introduce strong heterogeneity, show significant frequency dependence of Q_c . We note that reservations as to the validity of these correlations exist. For example, coda Q measurements in New England, USA (Pulli 1984), which is a non-tectonic region, show a very strong frequency dependence at lapse times less than $100 \, \mathrm{s}$.

The Q_c measurements in the eastern Caribbean exhibit a strong frequency dependence (n = 0.8-1.1), which if we assume the validity of the above correlation, would not be surprising because of the presence of a subduction zone. However, within the eastern Caribbean, there seems to be no obvious correlation between the level of seismic activity and Q_o/n since the most seismically active subregions (Leewards and the Trinidad/Tobago areas) have about the same n and slightly higher Q_o than the St Vincent/St Lucia area where seismic activity is significantly less. The Dominica region which may be slightly less seismically active than the Leewards and Trinidad/Tobago areas has a lower Q_o and higher n. The frequency dependence of Q_c in three subduction-zone environments in other parts of the world: Adak Islands, Aleutians (Scherbaum & Kisslinger 1985, 1987), Washington State, USA (Havskov et al. 1989) and Hindu Kush (Roecker et al. 1982), average about 60 for Q_o and 1 for n. The Q_o values in these areas are lower than those obtained in the eastern Caribbean.

Coda Q of local earthquakes recorded by short-period seismic stations on some eastern Caribbean islands was determined using the single-scattering model. The lateral and depth variation of Qc in the region seems to be relatively small. Qo is a minimum in the Dominica region $(Q_o = 97)$ and a maximum in the Leewards. $(Q_o = 145)$ while the degree of frequency dependence is largest in the Dominica area (n = 1.09) and smallest in the Leewards (n = 0.82). The possibility of the existence of site effects at stations such as ANG and NEV cannot be totally discounted. The use of shorter lapse times with the consequent sampling of shallower structures may have yielded larger regional variations. However, the similarity in average Q_c may be an indication that average attenuation properties in the crust and uppermost mantle in the eastern Caribbean are similar.

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